

Mathematics, Information, and Computer Sciences – School of STEM
MTH3003 Problem Solving
3 units
Fall 2024

Tuesdays and Thursdays **Liberty Station, Room 202** 

Final Exam: Main Room Liberty Station on Friday December 20th 1:30 pm – 4:00 pm

Section information:	Section information: Section 1 meets from 10:30-11:45am. Section 2 meets from 1-2:15pm	
Instructor information:	Kyle Havens, Assistant Professor of Professional Practice	
Phone:	619-849-2219	
Email:	kylehavens@pointloma.edu	
Office hours:	Location: Rohr Science 210  Monday and Wednesday: 1:00 pm – 2:15 pm  Tuesday and Thursday: 7:30 am – 10:00 am  Friday: 8:45 am – 9:45 am	

#### PLNU MISSION: TO TEACH ~ TO SHAPE ~ TO SEND

Point Loma Nazarene University exists to provide higher education in a vital Christian community where minds are engaged and challenged, character is modeled and formed, and service is an expression of faith. Being of Wesleyan heritage, we strive to be a learning community where grace is foundational, truth is pursued, and holiness is a way of life.

### **DEPARTMENT MISSION**

The Mathematical, Information, and Computer Sciences department at Point Loma Nazarene University is committed to maintaining a curriculum that provides its students with the tools to be productive, the passion to continue learning, and Christian perspectives to provide a basis for making sound value judgments.

### **GENERAL EDUCATION**

PLNU provides a foundational course of study in the liberal arts informed by the life, death, and resurrection of Jesus Christ. In keeping with the Wesleyan tradition, the curriculum equips students with a broad range of knowledge and skills within and across disciplines to enrich major study, lifelong learning, and vocational service as Christ-like participants in the world's diverse societies and culture.

#### **COURSE DESCRIPTION**

A general education course whose major goal is to develop the ability to solve non-routine problems through dynamic processes of inquiry and exploration, logical reasoning, making and testing conjectures and investigating implications of conclusions. A study of quantitative reasoning with emphasis on active problem solving and developing connections with other disciplines. Not applicable toward a major in Mathematics.

### PROGRAM AND COURSE LEARNING OUTCOMES

- Students will be able to formulate a mathematical model from a verbal description of a problem.
- Students will be able to solve non-routine problems using logic and quantitative techniques.
- Students will be able to construct solutions to problems using computational techniques

#### **GENERAL EDUCATION LEARNING OUTCOMES**

- Link to GE courses and corresponding GELO's: <a href="https://assessment.pointloma.edu/academic-assessment/general-education/assessment-plan/">https://assessment.pointloma.edu/academic-assessment/general-education/assessment-plan/</a>
- GELO 1e: Students will be able to solve problems that are quantitative in nature. A group project will be used to assess this learning outcome.
- Signature Assignment: Group Project

# REQUIRED TEXTS AND RECOMMENDED STUDY RESOURCES

**Textbook:** Excursion in Modern Mathematics, 10<sup>th</sup> Edition (Electronic Copy via My Lab and Mastering)

**Author:** Peter Tannenbaum **Publisher:** PEARSON

### **COURSE CREDIT HOUR INFORMATION**

In the interest of providing sufficient time to accomplish the stated Course Learning Outcomes, this class meets the PLNU credit hour policy for a 3-unit class delivered over 15 weeks. It is anticipated that students will spend a minimum of 37.5 participation hours per credit hour on their coursework. For this course, students will spend an estimated 112.5 total hours meeting the course learning outcomes. The time estimations are provided in the Canvas modules. Specific details about how the class meets the credit hour is provided below.

Online Homework	20.00
Written Homework	20:00
Reading Text/ Watching videos	30.00
Group Project	6.00
Budget Project	4.00
Class meetings	30.00
Midterms	2.50
Final Exam	2.50
TOTAL	115.00

#### ASSESMENT AND GRADING

The grade components are written homework, online homework, projects, collaborative activities, midterm exams, and the final examination.

### **GRADING SCALE**

A passing grade requires getting at least 60% in one of the two tests or on the final exam. Grades are based on the number of points accumulated throughout the course. Approximate minimal percentages required to obtain a given grade are:

Grading Scale in Percentages				
	А	ВСО		
+		(87.5, 90]	(77.5, 80]	(67.5, 70]
	(92.5, 100]	(82.5, 87.5]	(72.5, 77.5]	(62.5, 67.5]
_	(90, 92.5]	(80, 82.5]	(70, 72.5]	[60, 62.5]

#### **GRADING DISTRIBUTION**

Grade Distribution	
Two Mid Terms scored at 17.5%	35%
Final Exam (Cumulative)	25%
Online Assignments (OA)	10%
Group Project	5%
Individual Budget Assignment	5%
Written Homework	13%
Class Activities	7%
Total	100%

#### **FINAL EXAMINATION POLICY**

Successful completion of this class requires taking the final examination on its scheduled day. The final examination schedule is posted on the <u>Traditional Undergraduate Records: Final Exam Schedules</u> site. If you find yourself scheduled for three (3) or more final examinations on the same day, you are authorized to contact each professor to arrange a different time for <u>one</u> of those exams. However, unless you have three (3) or more exams on the same day, no requests for alternative final examinations will be granted.

#### **CONTENT WARNING**

I acknowledge that each of you comes to PLNU with your own unique life experiences. This contributes to the way you perceive various types of information. In Problem Solving, all of the class content, including that which may be intellectually or emotionally challenging, has been intentionally curated to achieve the learning goals for this course. The decision to include such material is not taken lightly. These topics include social choice, graph theory, and finance. If you encounter a topic that is intellectually challenging for you, it can manifest in feelings of discomfort and upset. In response, I encourage you to come talk to me or your friends or family about it. Class topics are discussed for the sole purpose of expanding your intellectual engagement in the area of mathematics, and I will support you throughout your learning in this course.

#### TRIGGER WARNING

I acknowledge that each of you comes to PLNU with your own unique life experiences. This contributes to the way you perceive several types of information. In Problem Solving, we will cover a variety of topics, some of which you may find triggering. These topics include social choice, graph theory, and finance. Each time this topic appears in a reading or unit, it is marked on the syllabus. The experience of being triggered versus intellectually challenged are different. The main difference is that an individual must have experienced trauma to experience being triggered, whereas an intellectual challenge has nothing to do with trauma. If you are a trauma survivor and encounter a topic in this class that is triggering for you, you may feel overwhelmed or panicked and find it difficult to concentrate. In response, I encourage you to take the necessary steps for your emotional safety. This may include leaving class while the topic is discussed or talking to a therapist at the Counseling Center. Should you choose to sit out on discussion of a certain topic, know that you are still responsible for the material; but we can discuss if there are other methods for accessing that material, and for assessing your learning on that material. Class topics are discussed for the sole purpose of expanding your intellectual engagement in the area of mathematics, and I will support you throughout your learning in this course

#### OTHER FACTORS THAT AFFECT GRADES

- Online Assignments: Online assignments (OA) will be completed in Access Pearson and Mastering website. This will be available by purchasing an access code.
- Written Homework: Assignments collected must be prepared in a style suitable for grading. The following guidelines are used to determine credit:
  - o the organization must be easy to follow
  - o the work must be legible
  - o complete solutions must be written for problems (not just answers); answers must be clearly marked
  - use complete sentences to answer questions
- Tests and Final Examination: Tests and the final exam will include problems and questions over material assigned in the text, readings and handouts, as well as material presented in class. No examination shall be missed without prior consent or a well-documented emergency beyond your control. A score of zero will be assigned for an examination that is missed without prior consent or a well-documented emergency beyond your control. The examination schedule is included in the daily schedule. This instructor does not intend to accept excuses such as poor communication with parents, benefactors, surf team sponsors and/or travel agents. The final exam date and time is set by the university at the beginning of the semester and may not be changed by the instructor. Only in the case that a student is required to take three exams during the same day of finals week is an instructor authorized to change the exam date and time for that particular student. The

student must contact each professor in order to work out an alternate time for one of those examinations. Department chairs/school deans and college deans need not be involved in the process of making this accommodation. Such accommodations and the negotiations necessary to arrange them must be completed at least four weeks prior to the official time of the final examination.

#### **INCOMPLETE AND LATE ASSIGNMENTS**

- All assignments are to be submitted/turned in by the beginning of the class session when they are due—
  including assignments posted in Canvas. Late work need not be accepted. Make-up tests will be given only by
  prior arrangement with the instructor for reasons of documented emergency.
- Incomplete grade: Incompletes will only be assigned in extremely unusual circumstances. You may request a grade of I (incomplete) only if you are having a passing grade and at least 70% of the course work is completed.

### Written Homework AT - A - GLANCE

These assignments are to be written up on paper or a PDF uploaded to CANVAS on or before the due date.

Chapter	Page	Problems	Due Date
1	29 – 37	# 4, 16, 30, 38, 50, 52	9/20/24
2	60 – 67	# 4, 18, 36, 58, 60, 64	9/27/24
4	126 – 134	# 4, 16, 20, 26, 34, 40	10/11/2024
5	162 – 171	# 6, 10, 30, 46, 54, 56	10/25/2024
6	194 – 203	# 6, 14, 34, 40, 44, 52	11/8/2024
7	219 – 225	# 6, 20, 26, 40, 42, 50	11/15/2024
8	246 – 255	# 30,36, 40, 54, 56, 58	11/22/2024
10	322 – 326	# 20, 36, 50, 60, 62, 70	12/13/2024

#### Comments on homework:

- 1. This is the minimum amount of homework that is required but you may need to do several odd numbered problems to make sure you get the answer in the textbook.
- 2. Be sure to upload a scanned copy of your homework before the deadline. No late homework will be accepted except by prior arrangement or with a documented emergency. Please be sure that your scanned homework is legible and not in HEIC format (PDF or JPEG are good).
- 3. Homework will be scored on a combination of completeness and correctness. All work necessary to complete a problem must be shown to earn credit.
- 4. Start working on your homework early. These problems are difficult and meant to be done a little at a time over the course of a few days.
- 5. When doing homework, please note it is normal to not be able to do every problem correct on the first attempt. Do not be discouraged, instead seek help.

### **SPIRITUAL CARE**

Please be aware PLNU strives to be a place where you grow as whole persons. To this end, we provide resources for our students to encounter God and grow in their Christian faith.

If you have questions, a desire to meet with the chaplain or have prayer requests you can contact the <a href="Office of Spiritual Life and Formation">Office of Spiritual Life and Formation</a>

### **STATE AUTHORIZATION**

State authorization is a formal determination by a state that Point Loma Nazarene University is approved to conduct activities regulated by that state. In certain states outside California, Point Loma Nazarene University is not authorized to enroll online (distance education) students. If a student moves to another state after admission to the program and/or enrollment in an online course, continuation within the program and/or course will depend on whether Point Loma Nazarene University is authorized to offer distance education courses in that

state. It is the student's responsibility to notify the institution of any change in his or her physical location. Refer to the map on <a href="State Authorization">State Authorization</a> to view which states allow online (distance education) outside of California.

### **PLNU COPYRIGHT POLICY**

Point Loma Nazarene University, as a non-profit educational institution, is entitled by law to use materials protected by the US Copyright Act for classroom education. Any use of those materials outside the class may violate the law.

### PLNU RECORDING NOTIFICATION

In order to enhance the learning experience, please be advised that this course may be recorded by the professor for educational purposes, and access to these recordings will be limited to enrolled students and authorized personnel.

Note that all recordings are subject to copyright protection. Any unauthorized distribution or publication of these recordings without written approval from the University (refer to the Dean) is strictly prohibited.

### PLNU ACADEMIC HONESTY POLICY

Students should demonstrate academic honesty by doing original work and by giving appropriate credit to the ideas of others. Academic dishonesty is the act of presenting information, ideas, and/or concepts as one's own when in reality they are the results of another person's creativity and effort. A faculty member who believes a situation involving academic dishonesty has been detected may assign a failing grade for that assignment or examination, or, depending on the seriousness of the offense, for the course. For all student appeals, faculty and students should follow the procedures outlined in the University Catalog. See <a href="Academic Policies">Academic Policies</a> for definitions of kinds of academic dishonesty and for further policy information.

### **ARTIFICIAL INTELLEGENCE (AI) POLICY**

You are allowed to use Artificial Intelligence (AI) tools (e.g., ChatGPT, Gemini Pro 1.5, GrammarlyGo, Perplexity, etc) to generate ideas, but you are not allowed to use AI tools to generate content (text, video, audio, images) that will end up in any work submitted to be graded for this course. If you have any doubts about using AI, please gain permission from the instructor.

### PLNU ACADEMIC ACCOMMODATIONS POLICY

PLNU is committed to providing equal opportunity for participation in all its programs, services, and activities in accordance with the Americans with Disabilities Act (ADA). Students with disabilities may request course-related accommodations by contacting the Educational Access Center (EAC), located in the Bond Academic Center (EAC@pointloma.edu or 619-849-2486). Once a student's eligibility for an accommodation has been determined, the EAC will work with the student to create an Accommodation Plan (AP) that outlines allowed accommodations. The EAC makes accommodations available to professors at the student's request.

PLNU highly recommends that students speak with their professors during the first two weeks of each semester/term about the implementation of their AP in that particular course. Accommodations are not retroactive so clarifying with the professor at the outset is one of the best ways to promote positive academic outcomes.

Students who need accommodations for a disability should contact the EAC as early as possible (i.e., ideally before the beginning of the semester) to assure appropriate accommodations can be provided. It is the student's responsibility to make the first contact with the EAC. Students cannot assume that because they had accommodations in the past, their eligibility at PLNU is automatic. All determinations at PLNU must go through the EAC process. This is to protect the privacy of students with disabilities who may not want to disclose this information and are not asking for any special accommodations.

### LANGUAGE OF BELONGING

Point Loma Nazarene University faculty are committed to helping create a safe and hospitable learning environment for all students. As Christian scholars we are keenly aware of the power of language and believe in treating others with dignity. As such, it is important that our language be equitable, inclusive, and prejudice free. Inclusive/Bias-free language is the standard outlined by all major academic style guides, including MLA, APA, and

Chicago, and it is the expected norm in university-level work. Good writing and speaking do not use unsubstantiated or irrelevant generalizations about personal qualities such as age, disability, economic class, ethnicity, marital status, parentage, political or religious beliefs, race, gender, sex, or sexual orientation. Inclusive language also avoids using stereotypes or terminology that demeans persons or groups based on age, disability, class, ethnicity, gender, race, language, or national origin. Respectful use of language is particularly important when referring to those outside of the religious and lifestyle commitments of those in the PLNU community. By working toward precision and clarity of language, we mark ourselves as serious and respectful scholars, and we model the Christ-like quality of hospitality.

If you (or someone you know) have experienced a bias incident regarding language, you can find more information on reporting and resources at www.pointloma.edu/bias.

#### SEXUAL MISCONDUCT AND DISCRIMINATION

In support of a safe learning environment, if you (or someone you know) have experienced any form of sexual discrimination or misconduct, including sexual assault, dating or domestic violence, or stalking, know that accommodations and resources are available through the Title IX Office at <a href="mailto:pointloma.edu/Title-IX">pointloma.edu/Title-IX</a>. Please be aware that under Title IX of the Education Amendments of 1972, faculty and staff are required to disclose information about such misconduct to the Title IX Office.

If you wish to speak to a confidential employee who does not have this reporting responsibility, you can contact Counseling Services at <a href="mailto:counselingservices@pointloma.edu">counselingservices@pointloma.edu</a> or find a list of campus pastors at <a href="mailto:pointloma.edu/title-ix">pointloma.edu/title-ix</a>.

If you (or someone you know) have experienced other forms of discrimination or bias, you can find more information on reporting and resources at <a href="https://www.pointloma.edu/bias">www.pointloma.edu/bias</a>

#### PLNU ATTENDANCE AND PARTICIPATION POLICY

Regular and punctual attendance at all class sessions is considered essential to optimum academic achievement. If the student is absent for more than 10 percent of class sessions, the faculty member will issue a written warning of de-enrollment. If the absences exceed 20 percent, the student may be de-enrolled without notice until the university withdrawal date or, after that date, receive an "F" grade.

- Online Courses: These are courses with class meetings where all instruction and interaction is fully online.
- Synchronous Courses: At least one class meeting takes place at a designated time.
- Asynchronous Courses: All class meetings are asynchronous.
- Hybrid Courses: These are courses with class meetings that take place both in the classroom and online synchronously and/or asynchronously.
- In-Person Courses: These are courses that meet in person with the instructor and students in a physical classroom setting. With approval by the area dean, this may include up to 25% of qualified class interactions through a Learning Management System (such as Canvas).

In some courses, a portion of the credit hour content will be delivered asynchronously and attendance will be determined by submitting the assignments by the posted due dates. See <u>Academic Policies</u> in the Undergraduate Academic Catalog.

#### **CLASS ENROLLMENT**

It is the student's responsibility to maintain his/her class schedule. Should the need arise to drop this course (personal emergencies, poor performance, etc.), the student has the responsibility to follow through (provided the drop date meets the stated calendar deadline established by the university), not the instructor. Simply ceasing to attend this course or failing to follow through to arrange for a change of registration (drop/add) may easily result in a grade of F on the official transcript.

#### **COURSE PHILOSOPHY**

The general method of the course is to involve students in "dynamic processes of inquiry and exploration, logical reasoning, making and testing conjectures, and investigating implications of conclusions" [Catalog]. Specifically,

the focus is on the processes and tools of quantitative problem solving. Learning what they are and developing ability to use them.

"Today's world is more mathematical than yesterday's, and tomorrow's world will be more mathematical than today's."

"...mathematics...serves as a key to opportunity and careers." [Everybody Counts, p.45, p.3]

"To participate rationally in a world where discussions about everything from finance to the environment, from personal health to politics, are increasingly informed by mathematics, one must understand mathematical methods and concepts, their assumptions and implications." [50 Hours, p.35]

In view of these statements and many other similar ones from national reports, this quantitative experience (MTH 3003) has been included as part of the PLNU general education curriculum. Thus, all students will study "major concepts, methods, and applications of quantitative reasoning with emphases on active problem solving" [Catalog].

### **COURSE APPROACH**

The ability to solve problems requires resourcefulness, flexibility, and efficiency in dealing with new obstacles. Research on teaching and learning problem solving suggests that certain factors are critical to successful problem solving, including resources, heuristics, control, and belief systems [Schoenfeld, 1985].

Resources refer to whatever information problem solvers understand (or misunderstand) that might be brought to bear on a problem.

Heuristic refers to strategies and techniques problem solvers have (or lack) for making progress when working on non-routine problems.

Control refers to the way problem solvers use (or fail to use) the information at their disposal.

Belief systems refer to the problem solver's "world view" of the problem domain, which determines the ways they use the knowledge in the first three categories.

The approach in MTH 3003 develops and uses these factors to increase your problem-solving ability. Classroom techniques used include:

- the teacher as role model
- whole-class problem solving with teacher as control
- small-group problem solving with teacher as coach

In addition, you are assigned readings and problems that will help you identify and make progress in the four areas discussed above.

# **COURSE METHODS**

- Use of groups: There is almost a century of research showing that academic achievement, productivity, and self-esteem improve dramatically when students work together in groups. This method emphasizes teamwork, cooperation and support by others, rather than isolation and competition in learning.
- Role of the classroom instructor: There will be less direct "lecturing" in class than usual, with many questions
  "answered" by another question to help you work through your own questions and difficulties. You are
  expected to learn problem solving through active involvement reading, writing, and explaining to others
  what you are thinking and doing.

This may require some adjustment in the way you think about teaching and learning. Initially, you may wish for more direct information and answers, but your patience and effort will be rewarded with a deeper understanding and increasing independence in problem solving, as well as confidence in your ability to tackle new problems.

THE FINAL EXAM IS A COMPREHENSIVE EXAMINATION. (December 20<sup>th</sup>, Friday, 1:30 – 4:00 pm LBRT Station) Successful completion of this class requires taking the final examination on its scheduled day.

The final exam date, time and place is set by the university at the beginning of the semester and may not be changed by the instructor. This schedule can be found on the university website and in the course calendar. No requests for early examinations will be approved. Only in the case that a student is required to take three exams during the same day of finals week, is an instructor authorized to consider changing the exam date and time for that particular student.

# **DAILY SCHEDULE**

Week of	<u>Tuesday</u>	<u>Thursday</u>	<b>Due This Week</b>	
9/2/2024	<u>Lecture:</u> Course Intro & Ch.1	<u>Lecture:</u> Chapter 1	Obtain Course Materials,	
	Intro to Voting Systems	Alternative Voting Methods	Register MyLab, IntroOA	
9/9/2024	<u>Lecture:</u> Chapter 1	<u>Lecture:</u> Chapter 2	Online Assignments 1.1-1.5	
	Fairness of Voting Methods	Intro to Weighted Voting	Class Activities Ch1	
0/16/2024	Lecture: Chapter 2	NO CLASS	OA1.6-2.1	
9/16/2024	Banzhaf Power Distribution	Professor Out Of Town	Written Homework Ch1	
0/22/2024	<u>Lecture:</u> Chapter 2	<u>Lecture:</u> Chapter 4	OA2.2-2.4	
9/23/2024	Shapley Shubik Power	Intro to Apportionment	CA2, WHW2	
0/20/2024	Lecture: Chapter 4	Lecture: Ch4 & Review	OA4.1-4.4	
9/30/2024	Modified Divisor Methods	Apportionment and Fairness	Class Activities Ch4	
	OPTIONAL	F-1	OA4.5-4.6	
10/7/2024	Office Hours	Exam #1	WHW4, Study	
10/14/2024	<u>Lecture:</u> Chapter 5	<u>Lecture:</u> Chapter 5	OA5.1-5.2	
10/14/2024	Intro to Graph Theory	Street Routing Problems	*Begin Group Project*	
10/21/2024	Lecture: Chapter 5	NO CLASS	OA5.3-5.4	
10/21/2024	Eulerizing and Solving SRPs	Fall Break	CA5, WHW5	
10/20/2024	Lecture: Chapter 6	<u>Lecture:</u> Chapter 6	OA6.1-6.4	
10/28/2024	Traveling Salesman Problems	Algorithms to Solve TSPs	CA6	
11/4/2024	Lecture: Chapter 7	<u>Lecture:</u> Chapter 7 & 8	OA6.3-7.2	
11/4/2024	Network Problems and Trees	Kruskal's Algorithm, Digraphs	CA7, WHW6	
	Lecture: Chapter 8	<u>Lecture:</u> Chapter 8	OA7.3-8.2	
11/11/2024	Digraphs and Task Processers	Priority Lists and Scheduling	WHW7	
44/40/2024	Lecture: Chapter 8 & Review	Evam #2	OA8.3-8.5	
11/18/2024	Critical Paths and Backflow	Exam #2	CA8, WHW8, Study	
11/25/2024	OPTIONAL	NO CLASS	*Danie Duduct Dusiest*	
	Office Hours	Thanksgiving Break	*Begin Budget Project*	
12/2/2024	Lecture: Chapter 10	Lecture: Chapter 10	OA10.1-10.2	
	Introduction to Finance	Interest and Retirement		
12/9/2024	Lecture: Chapter 10	<u>Lecture:</u> Ch10 & Review	OA10.3-10.5	
	Loan Payment, Amortization	Amortization and Review	CA10, WHW10, Study	
12/16/2024	NO CLASS		Final Exam	
12/10/2024	Finals	Friday 12/20 @ 1:30-4pm		

\*Project Deadlines TBD\*

#### **REFERENCES**

- Baron, J. B. and Sternberg, R. J. Teaching Thinking Skills: Theory and practice. (1987). New York: W. H.
   Freeman.
- Bransford, J. and Stein, B. (1984). The Ideal Problem Solver. New York: W. H. Freeman.
- Brown, Stephen I., and Marion I. Walter. (1983). The Art of Problem Posing. Hillsdale, NJ: Lawrence Erlbaum Associates.
- Cheney, L. (Ed.) (1989) 50 Hours (Cheney Report). HEW
- Curcio, F.R. (Ed.). (1987). Teaching and Learning: A problem solving focus. Reston, VA: NCTM.
- Duncker, K. (1945). On problem solving. Psychological Monographs 58, No. 5 Whole # 270.) Washington, DC: American Psychological Association.
- Dunham, William. (1990). Journey Through Genius: The great theorems of mathematics. New York: John Wiley & Sons.
- Eves, Howard. (1990). Foundations and Fundamental Concepts of Mathematics. 3rd ed. Boston: PWS-KENT.
- Eves, Howard. (1983). Great Moments in Mathematics. (2 vols.). The Mathematical Association of America.
- Gardner, Howard. (1985). The Mind's New Science. New York: Basic Books.
- Hofmann, J. E. (1957). The History of Mathematics. New York: Philosophical Library.
- Kilpatrick, Jeremy. (1987). "Problem Formulating: Where Do Good Problems Come From?" Cognitive Science and Mathematics Education, edited by Alan H. Schoenfeld, pp. 123-48. Hillsdale, NJ: Lawrence Erlbaum Associates.
- Kline, M. (1962). Mathematics: A Cultural Approach. Reading, MA: Addison-Wesley.
- Kline, M. (1953). Mathematics in Western Culture. New York: Oxford University Press.
- Krulik, S. (Ed.). (1980). Problem Solving in School Mathematics. 1980 Yearbook of the National Council of Teachers of Mathematics. Reston, VA: NCTM.
- National Research Council. (1989). Everybody Counts: A Report to the Nation on the Future of Mathematics Education. Washington, DC: National Academy Press.
- Newell, A., and Simon, H. (1972). Human Problem Solving. Englewood Cliffs, J: Prentice-Hall.
- Papert, S. (1980). Mindstorms: Children, computers, and powerful ideas. New York: Basic Books.
- Paulos, John A. (1988). Innumeracy: Mathematical illiteracy and its consequences. New York: Hill and Wang.
- Peterson, Ivars. (1988). The Mathematical Tourist. New York: Freeman.
- Peterson, Ivars. (1990). Islands of Truth: A mathematical mystery cruise. New York: Freeman.
- Polya, G. (1945). How To Solve It. Princeton: Princeton University Press.
- Polya, G. (1954). Mathematics and Plausible Reasoning (2 vols.). Princeton: Princeton University Press.
- Polya, G. (1962 [Vol. 1] and 1965 [Vol. 2]; combined paperback edition, 1981). Mathematical Discovery. New York: Wiley.
- Polya, G., & Kilpatrick, J. (Eds.). (1974). The Stanford Mathematics Problem Book with Hints and Solutions. New York: Teachers College Press.
- Rolf, Howard L. (1988). Mathematics. Dubuque, IA: Wm. C. Brown.
- Schoenfeld, A. (1985). Mathematical Problem Solving. New York: Academic Press.
- Schoenfeld, A. (Ed.). (1987). Cognitive Science and Mathematics Education. Hillsdale, NJ: Lawrence Erlbaum.Steen, Lynn A. (Ed.) (1990). On the Shoulders of Giants: New Approaches to Numeracy. Washington, D.C.: National Academy Press.
- Tannenbaum, P. & Arnold, R. (1992). Excursions in Modern Mathematics. Englewood Cliffs, NJ: Prentice-Hall.
- Taylor A. (1950). Mathematics and Politics. Strategy, Voting, Power, and Proof. Springer-Verlag.
- Wickelgren, W. (1974). How to Solve Problems. San Francisco: W. H. Freeman.